



B.Tech IV Semester Supplementary Examinations, December 2024

NUMERICAL METHODS
(ME)

Maximum Marks: 70

Date:17.12.2024

Duration: 3 hours

- Note:
- 1.This question paper contains two parts A and B.
 2. Part A is compulsory which carries 20 marks. Answer all questions in Part A.
 3. Part B consists of 5 Units. Answer any one full question from each unit which carries 10M.
 4. Each question carries 10 marks and may have a, b, c, d as sub questions.

Part-A

All the following questions carry equal marks (10X2M=20) Marks)		CO	Bloom Tx
1	Find any two initial positive roots of the equation $e^x \sin x = 1$	1	L1
2	Define root of an equation	1	L1
3	If the interval of differencing is unity prove that $\Delta[x(x+1)(x+2)(x+3)]=4(x+1)(x+2)(x+3)$	2	L1
4	Prove that $(1 + \nabla)(1 - \Delta) = 1$	2	L1
5	Write Stirling's formula to find the derivate of a function	3	L1
6	Write the Newton's Backward Difference formula to find the derivative of a function	3	L1
7	Find $y(0.2)$ for $\frac{dy}{dx} = x - y, y(0) = 1$ Eulers method.	4	L1
8	Given $\frac{dy}{dx} = -xy^2, y(0) = 2, Compute y(0.1)$ using Eulers Method.	4	L1
9	Write the one dimensional heat equation.	5	L1
10	Write Crank_Nicolson formula	5	L1

Part-B

Answer All the following questions. (5X10M=50Marks)		CO	Bloom Tx												
11	Find a positive root_of $x^3-x-1=0$ by bisection method. [10M]	1	L2												
OR															
12	Find a real root of the equation $x \cdot \log_{10} x = 1.2$ which lies between 2 and 3 by Regula Falsi method. [10M]	1	L2												
13	Use Lagranges interpolation formula to fit the unique polynomial $P(x)$ of degree 2 or less such that $P(1)=1, P(3)=27, P(4)=64$ [10M]	2	L2												
OR															
14	Find $y(25)$ using Gauss Forward Difference Formula to the following data $y_{20}=24 ; y_{24}=32 ; y_{28}=35 ; y_{32}=40$ [10M]	2	L2												
15	Find $f'(1.72)$ and $f'(1.76)$ for the table given below [10M]	3	L2												
<table border="1" style="width: 100%; border-collapse: collapse; margin-left: 20px;"> <tbody> <tr> <td style="width: 5%;">x</td> <td style="width: 15%;">1.72</td> <td style="width: 15%;">1.73</td> <td style="width: 15%;">1.74</td> <td style="width: 15%;">1.75</td> <td style="width: 15%;">1.76</td> </tr> <tr> <td>y</td> <td>0.17907</td> <td>0.17728</td> <td>0.17552</td> <td>0.17377</td> <td>0.17204</td> </tr> </tbody> </table>		x	1.72	1.73	1.74	1.75	1.76	y	0.17907	0.17728	0.17552	0.17377	0.17204		
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y	0.17907	0.17728	0.17552	0.17377	0.17204										

	OR																																						
16	Dividing the range into 10 equal parts, find the approximate value of $\int_0^\pi \sin x \, dx$ by (i) Trapezoidal Rule (ii) Simpson's Rule [10M]	3	L2																																				
17	Solve $\frac{dy}{dx} = x^2 + y, y(0) = 1$ by Modified Eulers method and compute $y(0.2), y(0.4)$. [10M]	4	L2																																				
	OR																																						
18	Solve $\frac{dy}{dx} = xy$ using R-K method for $x=0.2$, given $y(0)=1, y'(0) = 0$ taking $h=0.2$ [10M]	4	L2																																				
19	Solve the Poisson equation $u_{xx}+u_{yy} = -81xy$, $0 < x < 1, 0 < y < 1$ given that $u(0,y)=0, u(x,0)=0, u(1,y)=100, u(x,1)=100$ and $h=1/3$ [10M]	5	L2																																				
	OR																																						
20	Solve the Laplace equation $u_{xx}+u_{yy}=0$ given that [10M]	5	L2																																				
	<table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>0</td> <td></td> <td>11.1</td> <td>17</td> <td>19.7</td> <td>18.6</td> </tr> <tr> <td>0</td> <td></td> <td>u1</td> <td>u2</td> <td>u3</td> <td>21.9</td> </tr> <tr> <td>0</td> <td></td> <td>u4</td> <td>u5</td> <td>u6</td> <td>21</td> </tr> <tr> <td>0</td> <td></td> <td>u7</td> <td>u8</td> <td>u9</td> <td>17</td> </tr> <tr> <td>0</td> <td></td> <td></td> <td></td> <td></td> <td>9</td> </tr> <tr> <td></td> <td></td> <td>8.7</td> <td>12.1</td> <td>12.5</td> <td></td> </tr> </table>	0		11.1	17	19.7	18.6	0		u1	u2	u3	21.9	0		u4	u5	u6	21	0		u7	u8	u9	17	0					9			8.7	12.1	12.5			
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