



**B.Tech II Semester Supplementary Examinations, June 2024**

**Engineering Mathematics-II**  
 (Common to CE,EEE,ME,ECE,CSE & IT)

**Maximum Marks: 70**

Date:24.06.2024 Duration: 3 hours

- Note:**
1. This question paper contains two parts A and B.
  2. Part A is compulsory which carries 20 marks. Answer all questions in Part A.
  3. Part B consists of 5 Units. Answer any one full question from each unit which carries 10M.
  4. Each question carries 10 marks and may have a, b, c, d as sub questions.

**Part-A**

All the following questions carry equal marks		(10X2M=20 Marks)	CO	Bloom Tx
1	Solve $(x^2 + y^2) dx + 2xy dy = 0$		1	L1
2	Find the orthogonal trajectories of the family of curves $y=mx$		1	L1
3	Solve $(D^2 + 9) y = 0$		2	L1
4	Find the P.I of $f(D) y = Q(x)$ where $Q(x) = \sin bx$ (or) $\cos bx$ , where 'b' is a constant.		2	L1
5	Find $L \{ \cos^2 4t \}$		3	L1
6	Find $L^{-1} \{ 1/s \}$		3	L1
7	Find $\nabla (x^2 + y^2 z)$		4	L1
8	Prove that $\vec{F} = yz\mathbf{i} + zx\mathbf{j} + yx\mathbf{k}$ is irrotational.		4	L1
9	If $\vec{F} = 3xy\mathbf{i} - y^2\mathbf{j}$ evaluate $\int_c \vec{F} \cdot d\vec{r}$ where 'c' is the curve $y = 2x^2$ in the xy-plane From (0,0) to (1,2)		5	L1
10	State Green's theorem.		5	L1

**Part-B**

Answer All the following questions.		(5X10M=50Marks)		
11	Solve $xy(1 + xy^2) dy/dx = 1$ [10M]		1	L2
OR				
12	The number 'N' of bacteria in a culture grew at a rate proportional to 'N'. The value of 'N' was initially 100 and increased to 332 in 1 hour. What was the value of 'N' after 1.5 hours? [10M]		1	L2
13	Solve $(D^2 - 4D + 4) y = 8x^2 e^{2x} \sin 2x$ [10M]		2	L2
OR				
14	$(x+1)^2 \frac{d^2y}{dx^2} - 3(x+1) \frac{dy}{dx} + 4y = x^2 + x + 1$ [10M]		2	L2
15	Find Laplace transform of $te^{3t} \cos 2t$ [10]		3	L2

	OR		
16	Find Inverse Laplace transform of $\frac{3s+7}{s^2-2s-3}$ . [10]	3	L2
17	(a) Prove that $\nabla(r^n) = nr^{n-2}\vec{r}$ [5M] (b) Find the directional derivative of $\phi(x, y, z) = x^2yz + 4xz^2$ at the point (1,-2,-1) in the direction of the normal to the surface $f(x, y, z) = x \log z - y^2$ at (-1,2,1). [5M]	4	L2
	OR		
18	Show that the vector $(x^2 - yz)i + (y^2 - zx)j + (z^2 - xy)k$ is irrotational and find its scalar potential. [10M]	4	L2
19	If $\vec{F} = (2x^2 - 3z)i - 2xyj - 4xk$ then evaluate $\int_v \nabla \cdot \vec{F} dv$ where 'v' is the closed region bounded by $x=0, y=0, z=0, 2x+2y+z=4$ [10M]	5	L2
	OR		
20	Verify Stoke's theorem for $\vec{F} = yi + zj + xk$ and surface is the part of sphere $x^2 + y^2 + z^2 = 1$ above the xy-plane. [10M]	5	L2