



(5X10M=50Marks)

2	<p>A. Find the rank of</p> $\begin{bmatrix} 1 & 4 & 3 & -2 & 1 \\ -2 & -3 & -1 & 4 & 3 \\ -1 & 6 & 7 & 2 & 9 \\ -3 & 3 & 6 & 6 & 12 \end{bmatrix}$ <p>reducing to echelon form.</p> <p style="text-align: right;">[5M]</p> <p>B. Discuss for what values of λ, μ the simultaneous equations $x + y + z = 6, x + 2y + 3z = 10, x + 2y + \lambda z = \mu$ have (i) no solution (ii) a unique solution (iii) an infinite number of solutions.</p> <p style="text-align: right;">[5M]</p>	CO1	1,2 6
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	OR		
3	<p>A. Find the inverse of $A = \begin{bmatrix} -2 & 1 & 3 \\ 0 & -1 & 1 \\ 1 & 2 & 0 \end{bmatrix}$ using Gauss Jordan method. [5M]</p> <p>B. Determine whether the following equations have a non-trivial solution, if so solve them: $x + 2y + 3z = 0, 3x + 4y + 4z = 0, 7x + 10y + 12z = 0$. [5M]</p>	CO1	3
4	<p>Verify Cayley-Hamilton theorem for the following matrix and hence find A^{-1} and A^4 where $A = \begin{bmatrix} 1 & 2 & -1 \\ 2 & 1 & -2 \\ 2 & -2 & 1 \end{bmatrix}$ [10M]</p>	CO2	3
	OR		
5	<p>Reduce the Quadratic form to a canonical form by an orthogonal reduction and discuss its rank, nature, index and signature $x^2 + 5y^2 + z^2 + 2xy + 2yz + 6zx$. [10M]</p>	CO2	3
6	<p>A. Solve $x \frac{dy}{dx} + y = x^3 y^6$. [5M]</p> <p>B. Find the orthogonal trajectories of the family of curves $x^{\frac{2}{3}} + y^{\frac{2}{3}} = a^{\frac{2}{3}}$, where a is the parameter. [5M]</p>	CO4	3
	OR		
7	<p>A. Solve $(x + 1) \frac{dy}{dx} - y = e^{3x}(x + 1)^2$. [5M]</p> <p>B. Show that the family of parabolas $x^2 = 4a(y + a)$ is self-orthogonal. [5M]</p>	CO3	5,6
8	<p>A. Solve $(D^2 + 2D + 2)y = e^{-x} + \sin 2x$. [5M]</p> <p>B. Solve $(D^3 - 3D - 2)y = x^2$. [5M]</p>	CO4	3
	OR		
9	<p>Solve by the method of variation of parameters $(D^2 - 2D)y = e^x \sin x$ [10M]</p>	CO4	3
10	<p>A. Evaluate $\iint y \, dx \, dy$ over the region R, where R is the region bounded by the parabolas $y^2 = 4x$ and $x^2 = 4y$. [5M]</p> <p>B. Evaluate $\iint r^2 \sin \theta \, dr \, d\theta$ over the semi-circle $r = 2a \cos \theta$ above the initial line. [5M]</p>	CO5	5
	OR		
11	<p>By Changing the order of integration, evaluate $\int_0^1 \int_0^{\sqrt{1-x^2}} y^2 \, dy \, dx$ [10M]</p>	CO5	5