



R20 Regulation **Subject code: 3B3AA**
TKR COLLEGE OF ENGINEERING AND TECHNOLOGY
 (Autonomous, Accredited by NAAC with 'A+' Grade)
B.Tech III Semester Supplementary Examinations, July 2024

NUMERICAL METHODS
(Civil Engineering)

Maximum Marks: 70

Date: 18.07.2024 Duration: 3 hours

- Note:
1. This question paper contains two parts A and B.
 2. Part A is compulsory which carries 20 marks. Answer all questions in Part A.
 3. Part B consists of 5 Units. Answer any one full question from each unit which carries 10M.
 4. Each question carries 10 marks and may have a, b, c, d as sub questions.

Part-A

All the following questions carry equal marks		(10X2M=20 Marks)	CO	Bloom Tx							
1	Write about Bisection method.		1	L1							
2	Find any two initial positive roots of the equation $xe^x = 2$		1	L1							
3	Find the relation between the operators E and D		2	L1							
4	Find the Lagrange's Interpolating polynomial fits the data <table border="1" style="margin: 5px auto; border-collapse: collapse;"> <tr> <td style="padding: 2px 5px;">x</td> <td style="padding: 2px 5px;">0</td> <td style="padding: 2px 5px;">1</td> <td style="padding: 2px 5px;">2</td> </tr> <tr> <td style="padding: 2px 5px;">f(x)</td> <td style="padding: 2px 5px;">2</td> <td style="padding: 2px 5px;">1</td> <td style="padding: 2px 5px;">12</td> </tr> </table>	x	0	1	2	f(x)	2	1	12	2	L1
x	0	1	2								
f(x)	2	1	12								
5	Evaluate $\int_0^1 x^3 dx$ by Trapezoidal Rule taking n=4		3	L1							
6	Write the formula of Simpson's $\frac{1}{3}$ rule		3	L1							
7	Write the formula for Taylor's series method and find an approximate value of y at x = 0.1 for $y' = e^x$, $y(0) = 0$.		4	L1							
8	Use Runge-kutta method of second order to find y(0.1) for the IVP $dy/dx = -y$, $y(0) = 1$.		4	L1							
9	What is the classification of equation $f_{xx} + 2f_{xy} + f_{yy} = 0$		5	L1							
10	Classify the equation $(1 + x^2)u_{xx} + (5 + 2x^2)u_{xy} + (4 + x^2)u_{yy} = 0$		5	L1							

Part-B

Answer All the following questions.		(5X10M=50Marks)													
11	Find a real root for $x e^x = \cos x$, using Regula Falsi method. [10]		1	L2											
OR															
12	Evaluate $\sqrt{28}$ to four decimal places by Newton's Raphson Method. [10]		1	L2											
13	Use Newton forward interpolation formula to compute the pressure of the steam at temperature 142°C from the following steam table. [10] <table border="1" style="margin: 5px auto; border-collapse: collapse;"> <tr> <td style="padding: 2px 5px;">temp</td> <td style="padding: 2px 5px;">140</td> <td style="padding: 2px 5px;">150</td> <td style="padding: 2px 5px;">160</td> <td style="padding: 2px 5px;">170</td> <td style="padding: 2px 5px;">180</td> </tr> <tr> <td style="padding: 2px 5px;">Pressure</td> <td style="padding: 2px 5px;">3.685</td> <td style="padding: 2px 5px;">4.854</td> <td style="padding: 2px 5px;">6.302</td> <td style="padding: 2px 5px;">8.076</td> <td style="padding: 2px 5px;">10.225</td> </tr> </table>	temp	140	150	160	170	180	Pressure	3.685	4.854	6.302	8.076	10.225	2	L2
temp	140	150	160	170	180										
Pressure	3.685	4.854	6.302	8.076	10.225										
OR															

14	A curve passes through the points (0,18), (1,10), (3, -18), (6,90). Find the slope of the curve at x = 2. [10]	2	L2														
15	Find the first and second derivatives of the function tabulated below at the point x=1.5. [10]	3	L2														
	<table border="1"> <tr> <td>X</td> <td>1.5</td> <td>2.0</td> <td>2.5</td> <td>3.0</td> <td>3.5</td> <td>4.0</td> </tr> <tr> <td>Y</td> <td>3.375</td> <td>7.0</td> <td>13.625</td> <td>24.0</td> <td>38.875</td> <td>59.0</td> </tr> </table>	X	1.5	2.0	2.5	3.0	3.5	4.0	Y	3.375	7.0	13.625	24.0	38.875	59.0		
X	1.5	2.0	2.5	3.0	3.5	4.0											
Y	3.375	7.0	13.625	24.0	38.875	59.0											
OR																	
16	Use Trapezoidal rule with n=4 to estimate $\int_0^1 \frac{1}{1+x^2} dx$ [10]	3	L2														
17	Given $y' = x + \sin y$, $y(0) = 1$ compute $y(0.2)$ with $h = 0.2$ using Euler's modified method. [10]	4	L2														
OR																	
18	Given $\frac{dy}{dx} = \frac{1}{x^2+y}$, $y(4) = 4$ compute $y(4.2)$ using R-K method of 4 th order $h = 0.2$ [10]	4	L2														
19	Solve the equation $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$, subject to the initial condition $u(x,0) = \sin \pi x$, $0 \leq x \leq 1$ and the boundary conditions $u(0,t) = 0, u(1,t) = 0$. Carry out computations for the two levels taking $h=1/3, k=1/36$ [10]	5	L2														
OR																	
20	Find the solution of Poisson equation $\frac{\partial^2 u}{\partial t^2} + \frac{\partial^2 u}{\partial x^2} = 8x^2y^2$, for the square mesh of the figure given below with $u(x,y)=0$ on the boundary and mesh length =1 [10]	5	L2														