



B.Tech IV Semester Supplementary Examinations, July 2024

NUMERICAL METHODS
(Common to CE & ME)

Maximum Marks: 70

Date:31.07.2024 Duration: 3 hours

- Note:
1. This question paper contains two parts A and B.
 2. Part A is compulsory which carries 20 marks. Answer all questions in Part A.
 3. Part B consists of 5 Units. Answer any one full question from each unit which carries 10M.
 4. Each question carries 10 marks and may have a, b, c, d as sub questions.

Part-A

All the following questions carry equal marks		(10X2M=20 Marks)	CO	Bloom Tx
1	Find any two initial positive roots of the equation $e^x \sin x = 1$		1	L1
2	Define root of an equation		1	L1
3	If the interval of differencing is unity prove that $\Delta[x(x+1)(x+2)(x+3)] = 4(x+1)(x+2)(x+3)$		2	L1
4	Prove that $(1 + \nabla)(1 - \Delta) = 1$		2	L1
5	Write Stirling's formula to find the derivate of a function		3	L1
6	Write the Newton's Backward Difference formula to find the derivative of a function		3	L1
7	Find $y(0.2)$ for $\frac{dy}{dx} = x - y, y(0) = 1$ Eulers method.		4	L1
8	Given $\frac{dy}{dx} = -xy^2, y(0) = 2$, Compute $y(0.1)$ using Eulers Method.		4	L1
9	What is the classification of the equation $f_{xx} + 2f_{xy} + f_{yy} = 0$		5	L1
10	Write Crank_Nicolson formula		5	L1

Part-B

Answer All the following questions.		(5X10M=50Marks)		
11	Find a positive root of $x^3 - x - 1 = 0$ by bisection method. [10M]		1	L2
OR				
12	Find a real root of the equation $x \cdot \log_{10} x = 1.2$ which lies between 2 and 3 by Regula Falsi method. [10M]		1	L2
13	Use Lagranges interpolation formula to fit the unique polynomial $P(x)$ of degree 2 or less such that $P(1)=1, P(3)=27, P(4)=64$ [10M]		2	L2
OR				
14	Find $y(25)$ using Gauss Forward Difference Formula to the following data $y_{20}=24; y_{24}=32; y_{28}=35; y_{32}=40$ [10M]		2	L2

15	Find $f'(1.72)$ and $f'(1.76)$ for the table given below [10M]					3	L2	
	x	1.72	1.73	1.74	1.75			1.76
	y	0.17907	0.17728	0.17552	0.17377			0.17204
OR								
16	Dividing the range into 10 equal parts, find the approximate value of $\int_0^\pi \sin x \, dx$ by (i) Trapezoidal Rule (ii) Simpson's Rule [10M]					3	L2	
17	Solve $\frac{dy}{dx} = x^2 + y, y(0) = 1$ by Modified Eulers method and compute $y(0.2), y(0.4)$. [10M]					4	L2	
OR								
18	Apply 4th order Runge-Kutta method to find $y(0.1)$ & $y(0.2)$ given $y' = x - y, y(0)=1$. [10M]					4	L2	
19	Solve the Poisson equation $u_{xx} + u_{yy} = -81xy$, $0 < x < 1, 0 < y < 1$ given that $u(0,y)=0, u(x,0)=0, u(1,y)=100, u(x,1)=100$ and $h=1/3$ [10M]					5	L2	
OR								
20	Solve the partial differential equation $\nabla^2 u = -10(x^2 + y^2 + 10)$ over the square with sides $x=0=y, x=3=y$ with $u=0$ on the boundary and mesh length=1 [10M]					5	L2	